

## Determination of center of mass

### Force:

In physics a force is any interaction which tends to change the motion of an object.

In other words, a force can cause object with mass to change its velocity (which includes to begin moving from a state of rest)

The original form of Newton's second law states that the net force acting upon an object is equal to the rate at which its momentum changes with time.

$$F = ma$$

force                  mass                  acceleration

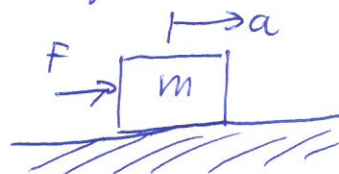
units

$F$  [N] - Newton

$m$  [kg] - kg

$a$  [ $\frac{m}{s^2}$ ]

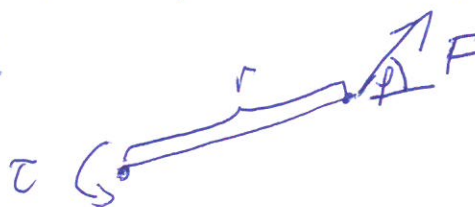
Sliding mass "translational"



### Torque

In other words torque, moment or moment of force is the tendency of a force to rotate an object about an axis (Just as a force is a push or a pull, a torque can thought of as a twist to an object).

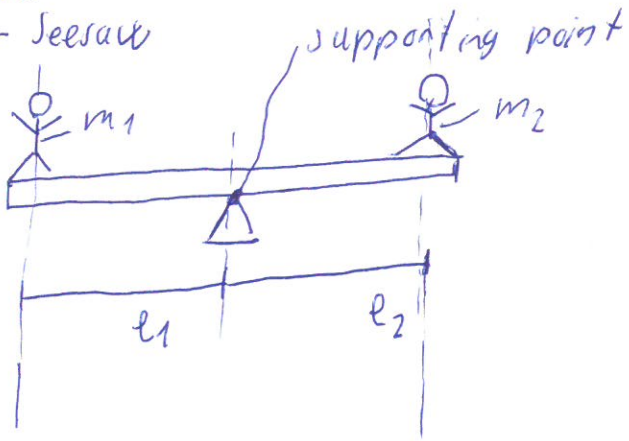
$$\tau = r \cdot \sin(\theta) \cdot F$$



$\sin 90^\circ = 1$

## Example

- Seesaw



$m_1$  is the mass of the first child

The children push the ~~see~~ seesaw with their own mass-force which is equal to  $m \cdot g$  where  $g$  is the gravitational acceleration / in the space no gravity the reason of free moving!

$$g = 9,81 \left[ \frac{m}{s^2} \right] \quad (\text{On the Earth})$$

The torque of the mass force respect to the supporting point

$$m_1 g \cdot l_1 \quad \& \quad m_2 g l_2$$

↑ the distance from the supporting point

For the equilibrium

$$m_1 g l_1 = m_2 g l_2$$

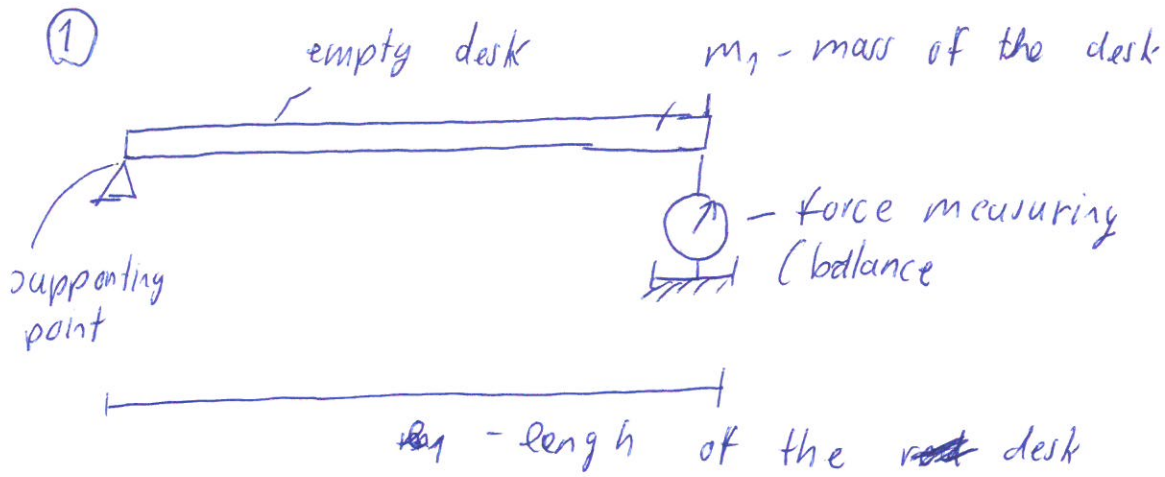
see = simple machines

„Lever“

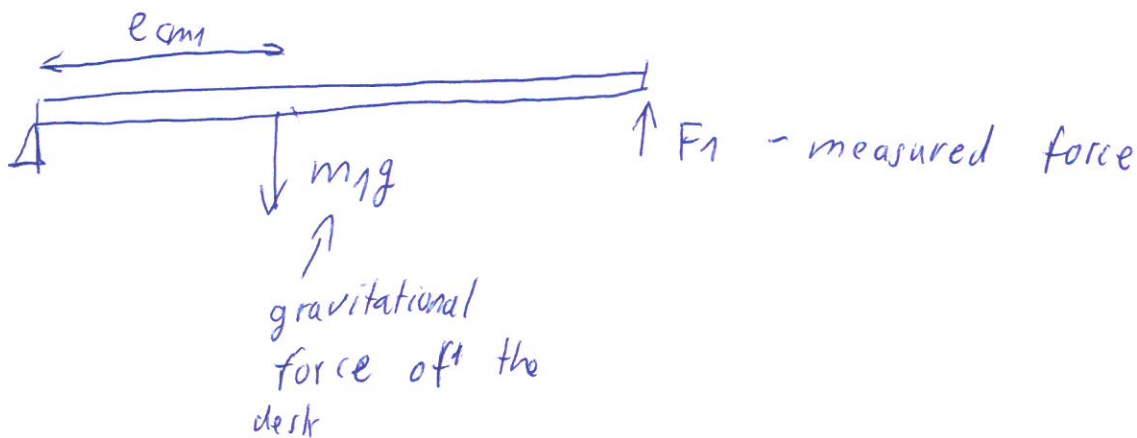
[en.wikipedia.org/wiki/Lever](http://en.wikipedia.org/wiki/Lever)

## Center of mass of lying body

The measurement setup



The gravitational force acting at the center of gravity  $l_{cm1}$



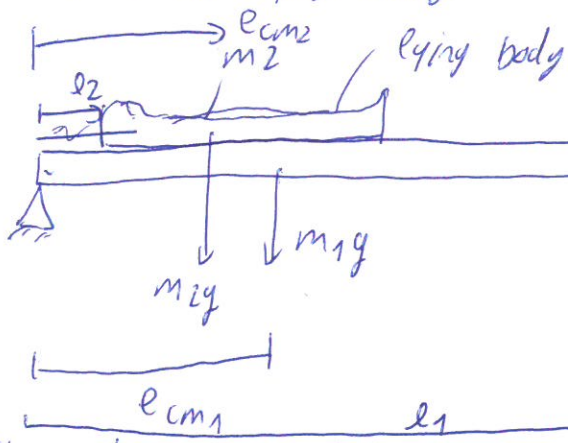
The torques of the forces respect to the supporting point should be equal

$$m_1g l_{cm1} = F_1 l_1$$

The place of the center of mass of the desk should be expressed

$$l_{cm1} = \frac{F_1 l_1}{m_1g}$$

(2) With the lying body



$F_2$  measured force

$m_2$  - mass of the body

The torques should be equal for the equilibrium / remember the seesaw)

$$m_1 g \cdot l_{cm1} + m_2 g \cdot l_{cm2} = F_2 \cdot l_1$$

$$l_{cm2} = \frac{F_2 \cdot l_1 - m_1 g \cdot l_{cm1}}{m_2 g}$$

the place of the center of mass in the global coordinate frame

The center of mass from the head

$$l_{cm2} - l_2$$